

Mark Scheme (Results)

January 2014

Pearson Edexcel International Advanced Level

Statistics 1 (WST01/01)



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General Marking Guidance

- Januarv 2014 W. Mynainscioud. com All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

EDEXCEL GCE MATHEMATICS

General Instructions for Marking

- 1. The total number of marks for the paper is 75.
- 2. The Edexcel Mathematics mark schemes use the following types of marks:
- **M** marks: method marks are awarded for `knowing a method and attempting to apply it', unless otherwise indicated.
- A marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
- **B** marks are unconditional accuracy marks (independent of M marks)
- Marks should not be subdivided.
- 3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes.

- bod benefit of doubt
- ft follow through
- the symbol $\sqrt{}$ will be used for correct ft
- cao correct answer only
- cso correct solution only. There must be no errors in this part of the question to obtain this mark
- isw ignore subsequent working
- awrt answers which round to
- SC: special case
- oe or equivalent (and appropriate)
- dep dependent
- indep independent
- dp decimal places
- sf significant figures
- ***** The answer is printed on the paper
- The second mark is dependent on gaining the first mark
- 4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.
- 5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected.
- 6. If a candidate makes more than one attempt at any question:
 - If all but one attempt is crossed out, mark the attempt which is NOT crossed out.
 - If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.
- 7. Ignore wrong working or incorrect statements following a correct answer.

	Januarv 20	14 MM 2 4	
Question Number	Scheme	Mar. ainsci	S
1. (a)	$S_{cs} = 380 - \frac{111 \times 21}{6} = -8.5$ o.e.	M1A1	Y.CON.
	$S_{ss} = 79 - \frac{21^2}{6} = 5.5$ o.e.	A1 (3)	
(b)	$r = \frac{S_{cs}}{\sqrt{S_{cc}S_{ss}}} = \frac{-8.5}{\sqrt{321.5 \times 5.5}} = -0.20214$ awrt -0.202	M1A1 (2)	
(c)	No evidence of, or weak, correlation (between cost and satisfaction) from data <u>or</u> evidence of negative correlation. [Allow <i>r</i> close to zero or $r < 0$] Poor basis for a decision, Brad is wrong or equivalent, e.g. "paying more doesn't give a better service"	B1ft, dB1ft	
		(2) Total 7	
	Notes		
(a)	M1 for a correct expression for S_{cs} or S_{ss}		
	1st A1 for $S_{cs} = -8.5$ (Condone $S_{xy} =$) accept $-\frac{17}{2}$ 2^{nd} A1 for $S_{ss} = 5.5$ (Condone S_{yy} or even $S_{xx} =$) accept $\frac{11}{2}$		
(b)	M1 for attempt at correct formula, values must be substituted. Must have their S_{cs} , S_{ss} and given S_{cc} in the correct places. Condone Award M1A0 for awrt -0.20 or even -0.2 with no expression seen M0 for $\frac{380}{\sqrt{79 \times 2375}}$ or $\frac{380}{\sqrt{79 \times 321.5}}$	missing "–"	
(c)	If Irl > 1 score B0B0 in (c) 1 st B1 for a reason: no or weak (or negative) correlation (between cost and This may be implied by a contextual statement e.g. "as he pays more satisfa	satisfaction) ction decreases"	
	2^{nd} d B1 dependent on suitable reason for saying that Brad ^{**} s decision is wron	g/bad/poor etc	
ft	If $0.5 < r \le 1$ allow the following ft 1 st B1 for positive correlation 2 nd dB1 for Brad ^{**} s decision is a good one		

		Januarv 20 ²	14 MM D	32
Question Number	Scheme		Mai	Altho Mar
2. (a)	$a = \frac{77 \times 1 + 82 \times 2 + \dots}{15} = \frac{1385}{15} = \frac{277}{3} = 92.\dot{3}$	awrt 92.3	M1 A1	SCIOU
	$b = [89.5 +] \frac{7.5 - 5}{9 - 5} (94.5 - 89.5) = 92.625$	awrt 92.6	M1 A1	
	$c = \frac{1 \times 77^2 + 2 \times 82^2 \dots}{15} - 92.\dot{3}^2 = 64.88\dots$	awrt 64.9	M1 A1	
				(6)
(b)	Median in 2010 (92.6 kg) > Median in 1990 (82.0 kg) Mean in 2010 (92.3 kg) > Mean in 1990 (83.0 kg) Rugby coach's claim supported.	either dep	B1 dB1	
		-	Total 8	(2)
	Notes			
a b From above	NB mid points are: 77, 82, 87, 92, 97 1 st M1 for attempt to use correct midpoints in an expression Accept $\frac{\sum fx}{15}$ with at least 3 correct fx products seen a or 1300 < $\sum fx < 1400$ 1 st A1 for awrt 92.3 (don"t insist on 3 sf) 2 nd M1 for $\frac{7.5-5}{9-5}(94.5-89.5)$ or $\frac{8-5}{9-5}(94.5-89.5)$ May see them come down from the top of the inter [94.5-] $\frac{9-7.5}{9-5}(94.5-89.5)$ or [94.5-] $\frac{9-7.5}{9-5}(94.5-89.5)$ Correct end point and [] not needed for M1 i.e. M1 is for correct 2 nd A1 for awrt 92.6 For $n + 1$ case (gives 93.25 so allow The correct answer must not follow from an incorrect	7, 102, 107 n for mean. and intention to a wal, look out for: $\frac{8}{-5}(94.5-89.5)$ fraction x corre awrt 93.3) Don" ect expression.	dd ct class widt t insist on 3	th 5 sf
С	3 rd M1 for a fully correct expression ft their <i>a</i> e.g. $\frac{128855}{15}$ 3 rd A1 for awrt 64.9 (Accept $s^2 = 69.5238$ or awrt 69.5)	$-a^2$ or $\frac{25771}{3}$ Don''t insist on 3	$-a^2$ sf	
(b)	1 st B1 for a suitable reason i.e. identifying an increase in m Ignore any comment about variance. 2 nd dB1 dependent on a suitable reason for stating that the cost Allow these marks provided both their $a > 83.0$ and If it is NOT the case that both $a > 83.0$ and $b > 82.0$ scored for both a and b in part (a)	the an or median ach''s claim is sup their $b > 82.0$ then allow a ft j	pported provided M	[1]

	Januarv 20	14 mm 14
Question Number	Scheme	Mar
3. (a)	$\begin{array}{c} p \\ 800 \\ 700 \\ 600 \\ 500 \\ 600 \\ 500 \\ 400 \\ 300 \\ 200 \\ 100 \\ 0 \end{array} \xrightarrow{\times} \begin{array}{c} \times \\ \times $	B2/1/0 -1eeoo
(b)	"Negative correlation" or "as <i>t</i> increases, <i>p</i> decreases" or "Points close to a straight line" or "linear correlation"	(2) B1
(c)	$b = \frac{S_{tp}}{S_u} = \frac{-6080}{254} (= -23.937)$ $a = \overline{p} - b\overline{t} = 470 + 23.937 \times 19.5 = 936.7717$ p = 936.7717 - 23.937t awrt $p = 937 - 23.9t$	(1) M1 M1, A1 A1
(d)	$p = 937.7717 - 23.937 \times 20, = 458.0315$ awrt (£) 458	(4) M1, A1
(e)	Extrapolation <u>or 39 (or</u> it"s) outside the range of data (or table) <u>BUT</u> B0 if they calculate p and say this is outside the range of the data Not a good decision <u>or</u> the prediction would be unreliable	(2) B1 dB1 (2) Total 11
	Notes	
(a)	1^{st} B1 for at least 7 points plotted correctly (i.e. within (not on) the circles 2^{nd} B1 for all 8 points plotted correctly (i.e. within (not on) the circles on the	on the overlay) e overlay)
(b)	B1 for a suitable comment conveying the idea of linear correlation NB "negative relationship" or "skew" scores B0 but apply ISW if a corre	ect ans. is seen
(c)	1^{st} M1for a correct expression for gradient b or awrt -24Allow fractions 2^{nd} M1for a correct method for a. Follow through their value for b Allow sign slip on b only if a correct formula for a is seen 1^{st} A1for a = awrt 937 2^{nd} A1for a correct equation in p and t (not x, y) with a = awrt 937 and b = awrt -2	e.g <u>3040</u> 3.9 <u>No fractions</u>
(d)	M1 for substituting $t = 20$ in their equation A1 for awrt 458 [NB use of 3sf for <i>a</i> and <i>b</i> will give awrt £459 but scores	s A0 here]
(e)	1^{st} B1 for a suitable reason that would lead to stating that the decision was p Stating that 39 is an "outlier" is B0 2^{nd} dB1 dependent on a suitable reason and stating, or implying, it is <u>not</u> a sensible	ooor/bad/wrong e decision

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Question Number	Scheme	Mang	Math.
4. (a)	$a + \frac{1}{10} + \frac{1}{5} + \frac{3}{10} + b = 1$ or $a + b = \frac{2}{5}$	M1	Sciouo.
	$-a + 0 + \frac{1}{5} + \frac{6}{10} + 3b = \frac{9}{5}$ or $3b - a = 1$	M1	
	Solving gives $a = \frac{1}{20}, b = \frac{7}{20}$	M1A1	
	x -1 0 1 2 3		(4)
(b)	$\begin{bmatrix} F(x) \end{bmatrix} \begin{array}{c cccc} 1 & 3 & 7 & 13 \\ \hline 20 & 20 & 20 & 20 \\ \hline 0.05 & 0.15 & 0.25 & 0.65 \\ \hline \end{array} $	B1B1 -1eeoo	
			(2)
(c)	$P(X < 2.5) = F(2) = \frac{13}{20}$ or 0.65	B1	
(b)	$E(X^2) = 1 \times 0.05 + 0 + 1 \times 0.2 + 4 \times 0.3 + 9 \times 0.35 = 4.6 \text{ or } \frac{23}{2}$	M1	(1)
(4)	$Var(X) = E(X^2) - 1.8^2$ [= 1.36 or $\frac{34}{25}$]	M1	
	$Var(3-2X) = (-2)^2 Var(X)$	M1	
	$=4 \times 1.36 = 5.44$ 5.44	A1	
		 Total 11	(4)
	Notes		
(a)	1^{st} M1for a correct linear equation in a and b based on sum of probs. = 1 2^{nd} M1for an attempt at a second linear equation in a and b based on $E(X) = 1.8$ Allow 3^{rd} M1for an attempt to solve their 2 linear equations. Must reduce to a linear one variable. May be implied by 1^{st} M1 and 2^{nd} M1 followed by correctA1dependent on all 3 Ms scored for $a = 0.05$ and $b = 0.35$ or exact fraction	w one slip. equation in t answers. 1 equivaler	n nts
ALT	State <i>a</i> and <i>b</i> correctly 1^{st} M1 for explicitly showing that sum of probs. = 1 2^{nd} M1 for explicitly showing that $E(X) = 1.8$ 3^{rd} M1 for an overall comment "therefore $a = \dots$ and $b = \dots$ " No comment loses this n	nark and A	1
(b)	1 st B1 for at least 4 correct values for $F(x)$ 2 nd B1 for all values of $F(x)$ correct Condone no $F(x)$ or even $P(x)$ if in a correct table. If not in a table they must state b	F(-1) = 0.05	5 etc
(d)	1 st M1 for an attempt to find $E(X^2)$. At least 3 correct terms or sight of 4.6 or co	orrect Var((X)
	NB $\frac{4.0}{5}$ loses the M1 for E(X^2) and the next M1 for Var(X) too		
	2^{nd} M1 for an attempt to find Var(X). Follow through their "4.6" but must see -3^{rd} M1 for correct use of Var($aX + b$) formula. Condone -2^2 if this later becom	-1.8^2 or 1. nes +4	.36
	A1 for 5.44 Accept $\frac{136}{25}$ or exact equivalent		

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Question Number	Scheme	Marks Cloud
5. (a)	$ \begin{array}{c c} S & \hline & & \\ \hline \\ \hline$	B1 B1 B1 B1 B1
(b)	F and S or R and S	$\begin{vmatrix} (4) \\ B1 \\ (1) \end{vmatrix}$
(c)	$P\left(\left[F \cup R \cup S\right]'\right) = \frac{33}{100} \text{ or } 0.33$	B1
(d)	$P(R) = \frac{30 + 12}{100} = \frac{21}{50} \text{or } \underline{0.42}$	(1) B1 (1)
(e)	$P(F \cup S) = \frac{30+25}{100} = \frac{11}{20} \text{ or } \underline{0.55}$	B1 (1)
(f)	$\left[P(F \mid R) \right] = \frac{P(F \cap R)}{P(R)} = \frac{"0.30"}{"0.42"}$	M1
	$=\frac{30}{42}$ or $\frac{5}{7}$ (o.e.)	A1 (2) Total 10
(a)	Notes	r intogors
(a)	1 st B1 for 3 labelled loops and a box. The 33 is not required for any marks in 2^{nd} B1 for $F \subset R$ or indicated by zeros 3 rd B1 for 30 and 12 correctly placed and $n(F) = 30$ and $n(F' \cap R) = 12$ 4 th B1 for S a separate loop, or indicated by zeros, and the 25	(a)
(b)	B1 for a correct pair. If there is more than one pair then each pair must be co Do not allow $P(F)$ etc or e.g. $P(R \cap S) = 0$	rrect.
(c),(d),(e)	B1 cao for each answer. Accept any exact equivalent (fractions or decimals) probabilities	for the
(f)	M1 ft their "30" and their answer to (d). For a correct ratio of their probabilit correct ratio expression and at least one correct probability. If num > den A1 for $\frac{5}{2}$ or any exact equivalent. Must be proper fraction not $\frac{0.3}{2}$	ties or a score M0
	NB $\frac{0.3}{0.42} = 0.714$ is A0 since it is not a proper fraction and the answer is n	not exact
	Condone P(R F) = $\frac{30}{42}$ and allow M1A1 for the correct answer	
	but $P(R F) = \frac{P(R \cap F)}{P(F)} = \frac{0.30}{0.42} = \frac{30}{42}$ is M0A0	

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Question Number	Scheme	Mark. Scio
6. (a)	$[X \sim N(1.04, 0.17^2)]$	Jul.
	$P(X < 1) = P\left(Z < \frac{1 - 1.04}{0.17}\right)$	M1
	= P(Z < -0.23529) = 1-0 5948 = 0 4052 (Accept 0 405-0 407)	MIA1
		(3)
(b)	$P(Y < 1) = 0.05$ $\left[Y \sim N(\mu, 0.17^2) \right]$	
	$\frac{1-\mu}{0.17} = -1.6449$	M1 B1
	$\mu = 1 + 1.6449 \times 0.17 = 1.2796 \dots$ awrt 1.28	A1
(c)	$P(S < 1) = 0.01$ $\left[S \sim N(1.04, \sigma^2) \right]$	(3)
	$\frac{1-1.04}{\sigma} = -2.3263$	M1B1
	$\sigma = \frac{0.04}{2.3263} = 0.0171946$ awrt 0.0172	A1
	2.5205	(3) Total 9
	Notes	
(a) (b)	$\begin{array}{ccc} 2^{nd} & \text{M1} & \text{for attempting to standardise with 1, 1.04 and 0.17} & \text{Anow} \pm 2^{nd} & \text{M1} & \text{for attempting 1} - p \text{ where } (0.5$	z value (z > 1) t allow 1 – 1.6449
Ans only	If answer is awrt 1.28 score M1B0A1 (unless of course $z = 1.6449$ seen) but awrt 1.2	2796 scores 3/3
(c)	M1 for an attempt to standardise with 1, 1.04 and σ and set = \pm any z value (B1 for $z = \pm 2.3263$ (or better) (Calc gives 2.3263478) used as a z value If B0 scored in (b) for using a value in [1.64, 1.65] but not 1.6449 or better, allow awn A1 for awrt 0.0172 Must follow from correct working but a range of possible	z > 2) et 2.32 or 2.33 here e z values are OK
Ans only	If answer is awrt 0.0172 score M1B0A1 (unless of course $z = 2.3263$ or be If B1 scored in (b) and $z = 2.3263$ or better is <u>not</u> seen here then require an range 0.17194 < σ < 0.17195 to award 3/3	etter is seen) n answer in the

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Question Number	Scheme	Mar	math
7. (a)	$[P(M L) =] \frac{P(M \cap L)}{P(L)} = \frac{\frac{3}{5} \times \frac{1}{5}}{\frac{3}{10}}$	M1	
	= 0.40 (o.e)	A1	(2)
(b)	$x = [P(L F)] = \frac{P(L \cap F)}{P(F)} = \frac{\frac{3}{10} - \frac{3}{5} \times \frac{1}{5}}{1 - \frac{3}{5}} \text{ or } \frac{3}{5} \times \frac{1}{5} + \left(1 - \frac{3}{5}\right) \times x = \frac{3}{10}$	M1	(2)
	$x = \frac{0.3 - 0.12}{0.40}$ or $0.4x = 0.3 - 0.12$	M1	
	x = 0.45 (o.e.)	A1	(3)
(c)	$[P(M \cap R)] = 0.6 - P(M \cap L) \qquad \underline{\text{or}} \qquad 0.6 \times (1 - 0.2)$	M1	(3)
	= <u>0.48</u> (o.e.)	A1	(2)
(d)	P(one is left handed and the other right handed) = $2 \times \frac{3}{10} \times \frac{7}{10} = \frac{21}{50}$ or 0.42	M1, A1	
		Total 9	(2)
	Notes		
(a)	If numerator > denominator then M0 A1 for 0.40 or any exact equivalent	reet proo	
(b)	1 st M1 for an equation for x with at least 2 of : $\left(\frac{3}{5} \times \frac{1}{5}\right)$ or $\frac{3}{10}$ or $\left(1 - \frac{3}{5}\right)$ corre	ct	
	BUT $\frac{\frac{2}{5} \times \frac{3}{10}}{\frac{2}{5}}$ is M0 <u>or</u> allow M1 for $P(L \cap F) = 0.18$		
	2^{nd} M1 for a fully correct expression for $x =$ or $0.4x =$ A1 for 0.45 or any exact equivalent		
(c)	M1 for a correct expression with 0.6 follow through their $P(M \cap L) = 0.12$ A1 for 0.48 or any exact equivalent		
(d)	M1 for a fully correct expression including the 2. Allow $1 - 0.3$ instead of (A1 for 0.42 or any exact equivalent).7	
	NB You may see Venn or tree diagram drawn but marks are given when used in correct expressions as above	n values a	are
	$M \underbrace{(0.48 \ 0.12 \ 0.18}_{0.22} L = \frac{3}{5} M \underbrace{(0.8)}_{0.2} R \\ \frac{3}{5} F \underbrace{(0.55)}_{2} R \\ \frac{2}{5} F \underbrace{(0.55)}_{1} R \\ \frac{3}{5} F \underbrace{(0.55)}$		

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uestion	Scheme	Mark	nar
8. (a)	Total area of bars = 400 small squares Area required = $40 \times 4 + 20 \times 6 + 6 \times 10 = 340$ small squares	B1 B1	- '5
	No of staff = "340" $\times \frac{40}{"400"}$, = 34	M1, A1	
(b)	Median is $(2+)\frac{4}{12} \times 3 = 3$ or $(5-)\frac{8}{12} \times 3 = 3$	M1A1	(4)
(c)	Mean is $\frac{\sum fx}{40} = \frac{1 \times 16 + 3.5 \times 12 + 7.5 \times 6 + 15 \times 4 + 25 \times 2}{40} = ,\frac{213}{40} = 5.325$	M1,A1	(2)
(d)	(Positive) skew but not negative <u>or</u> there are outliers (which affect mean) Median	B1 dB1	(2)
		Tota	l 10
(a)	Accept 160+120+60+40+20 or 80+60+30+20+10=200 or frequencies: 16 + or cm ² $6.4 + 4.8 + 2.4 + 1.6 + 0.8 = 16$ or key: 10 small squares = 2 nd B1 for a correct attempt to calculate required area (Accept 160 + 120 + or frequencies: 16 + 12 + 6 or cm ² $6.4 + 4.8 + 2.4 = 13.6$ M1 for a correct expression using their 400 and their 340 A1 for 34 If using frequencies they get M1A1 together when 34 is seen. An answer of 34 will usually score 4/4 unless there is incorrect work	5.e.) 12 + 6 + 4 1 person (o 60) ting seen	+ 2 .e.)
(b)	NB frequencies are: 16, 12, 6, 4, 2 and mid-points are: 1, 3.5, 7.5 M1 for $\frac{20-16}{12} \times (5-2)$ or $\frac{20.5-16}{12} \times (5-2)$ or similar expressions we Look out for methods based on areas should have 1 st bar + $\frac{1}{3}$ (2 nd bar) if (5 th + 4 th + 3 rd bars) + $\frac{2}{3}$ (2 nd bar) if working down. E.g. 16 + 4(x - 2) = A1 for 3 or (if using $n + 1$ accept 3.125 or awrt 3.13)	, 15, 25 orking down `working uj 20	n p <u>or</u>
(c)	M1 for an attempt at $\frac{\sum fx}{40}$ where at least 3 correct products of $\sum fx$ are so or $\sum fx = awrt 200 (1 sf)$	een	
	A1 for 5.325 or any exact equivalent e.g. $\frac{213}{40}$ and accept 5.33 Accept 5 h 19 mins or 5h 20 mins		
(d)	1 st B1 for a reason e.g. that the data is skewed Allow mention of "extreme values" or "outliers" Do not allow for <u>negative</u> skew or "anomalies"		
SC	2 nd dB1 dependent on mentioning skew for choosing <u>median</u> Allow B0B1 for "Choose median since the data has negative skew"	' o.e.	





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